

Closed book. No calculators are to be used for this quiz.

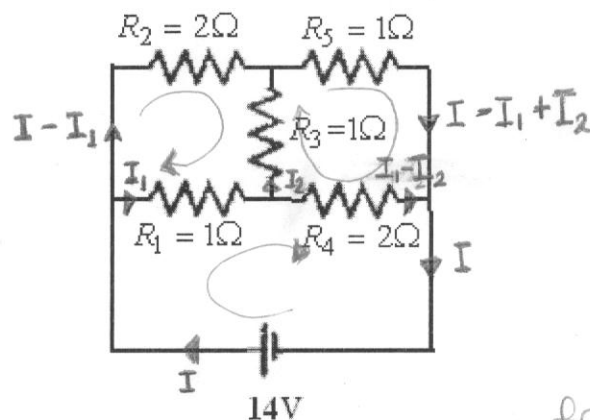
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

Find the current through each resistor in the circuit.



\* Current in the loops are determined via junction rule

bottom loop:

$$14V - I_1 \cdot 1\Omega - (I_1 - I_2) \cdot 2\Omega = 0$$

$$3I_1 + 2I_2 = 14 \quad (1)$$

top left loop:

$$-(I - I_1) \cdot 2\Omega + I_2 \cdot 1\Omega + I_1 \cdot 1\Omega = 0$$

$$-2I + 3I_1 + I_2 = 0 \quad (2)$$

top right loop:

$$-(I - I_1 + I_2) \cdot 1\Omega + (I_1 - I_2) \cdot 2\Omega + I_2 \cdot 1\Omega = 0$$

$$-I + 3I_1 - 4I_2 = 0 \quad (3)$$

from (1) - (2) we get:

$$2I - 3I_2 = 14 \quad (4)$$

from (3) - (2) we get

$$I - 5I_2 = 0$$

$$\Rightarrow I = 5I_2 \quad (5)$$

(Substitute (5) into (4):

$$7I_2 = 14A \Rightarrow I_2 = 2A$$

$$\Rightarrow I = 5I_2 = 10A$$

Solving (1) for  $I_1$  we find:

$$I_1 = \frac{14A + 2I_2}{3} = 6A$$

Thus,

$$I_{R1} = I_1 = 6A$$

$$I_{R2} = I - I_1 = 10A - 6A = 4A$$

$$I_{R3} = I_2 = 2A$$

$$I_{R4} = I - I_1 = 2A$$

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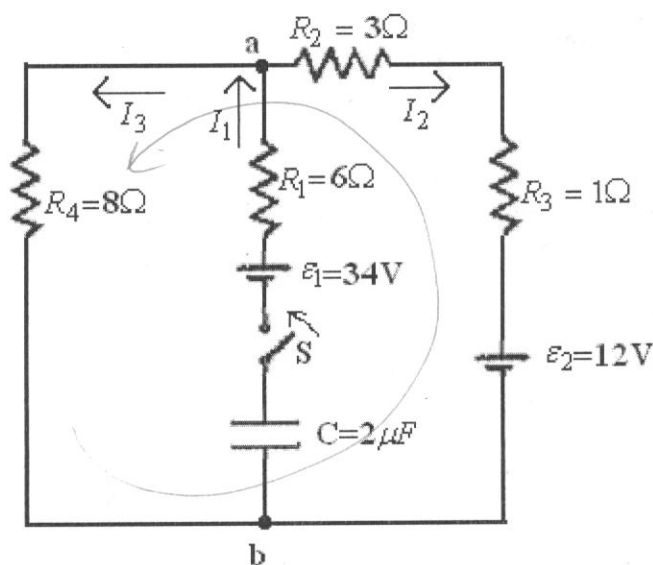
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Consider the circuit given in the figure. The capacitor is initially uncharged and the switch S is closed at  $t=0$ . Long time after ( $t$  goes to infinity) the switch S is closed, find the potential difference  $V_a - V_b$ . What is the maximum charge on the  $2 \mu\text{F}$  capacitor?



If we wait enough, the capacitor is fully charged. Then, the capacitor behaves as open circuit. ( $I_1 = 0$ )

The current flows from the outer loop only

$$12V + I_2 \cdot 1\Omega + I_2 \cdot 3\Omega - I_3 \cdot 8\Omega = 0$$

$$2I_2 - I_3 = 3A$$

Due to junction rule:  $I_1 = I_2 + I_3$  &  $I_1 = 0$

$$I_2 = -I_3$$

$$2I_3 - (-I_3) = 3A \Rightarrow$$

$$I_3 = 1A$$

$$I_2 = -1A$$

$$I_1 = 0$$

Potential across the capacitor

$$\text{is: } V_{ab} = I_3 \cdot R_4 = 1A \cdot 8\Omega = 8V$$

$$Q_{\text{max}} = C \cdot V = 2\mu\text{F} \cdot 8V = 16\mu\text{C}$$

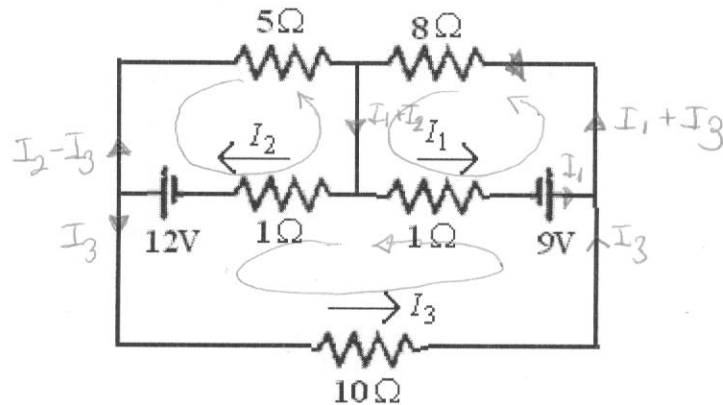
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Calculate the three currents  $I_1$ ,  $I_2$  and  $I_3$  indicated in the circuit diagram.



★ The currents in the branches are written due to junction rule!

Top left loop:

$$-12V + I_2 \cdot 1\Omega + (I_2 - I_3) \cdot 5\Omega = 0$$

$$6I_2 - 5I_3 = 12A \quad (1)$$

Top right loop:

$$-I_1 \cdot 1\Omega + 9V - (I_1 + I_3) \cdot 8\Omega = 0$$

$$9I_1 + 8I_3 = 9A \quad (2)$$

Bottom loop:

$$-I_3 \cdot 10\Omega - 9V + I_1 \cdot 1\Omega - I_2 \cdot 1\Omega + 12V = 0$$

$$-I_1 + I_2 + 10I_3 = 3A \quad (3)$$

Solve (1) for  $I_2$ :  $I_2 = 2A + \frac{5}{6}I_3$   
 Solve (2) for  $I_1$ :  $I_1 = 1A - \frac{8}{9}I_3$

Substitute into (3)

$$-(1A - \frac{8}{9}I_3) + (2A + \frac{5}{6}I_3) + 10I_3 = 3A$$

$$\frac{8}{9}I_3 + \frac{5}{6}I_3 + \frac{100}{10}I_3 = 2A$$

(2)      (3)      (1.8)

$$\left(\frac{16+15+180}{18}\right) I_3 = 2A \Rightarrow I_3 = 0.171A$$

Then:

$$I_2 = 2A + \frac{5}{6}(0.171A) = 2.14A$$

$$I_1 = 1A - \frac{8}{9}(0.171A) = 0.48A$$

$$I_1 = 0.48A$$

$$I_2 = 2.14A$$

$$I_3 = 0.171A$$

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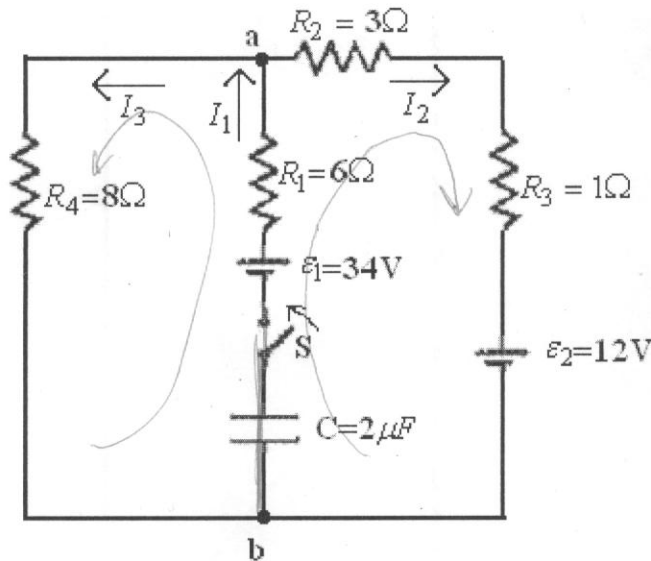
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Consider the circuit in given the figure. The capacitor is initially uncharged and the switch S is closed at  $t=0$ . Find the currents  $I_1$ ,  $I_2$  and  $I_3$  just after the switch S is closed.



Since the capacitors are initially uncharged, just after the switch is closed the potential across the capacitor is zero:

$$V_c = Q/C = 0 \quad (1)$$

The capacitor behave as an short circuit.

Left loop:  $34 - 6I_1 - 8I_3 = 0 \rightarrow 3I_1 + 4I_3 = 17A \quad (2)$

Right loop:  $34 - 6I_1 - 3I_2 - I_2 = 12 = 0 \rightarrow 3I_1 + 2I_2 = 22A \quad (3)$

Junction Rule:  $I_1 = I_2 + I_3 \quad (3)$

Substitute (3) into (1) & (2)

$$3I_2 + 3I_3 + 4I_3 = 17A \rightarrow 3I_2 + 7I_3 = 17A$$

$$3I_2 + 3I_3 + 2I_2 = 22A \rightarrow 5I_2 + 3I_3 = 22A$$

$$26I_3 = 52A$$

$$\Rightarrow I_3 = 2A$$

$$3I_1$$

$$3I_1 + 4I_3 = 17A \Rightarrow I_1 = 3A \quad \& \quad I_2 = I_1 - I_3 = 1A$$

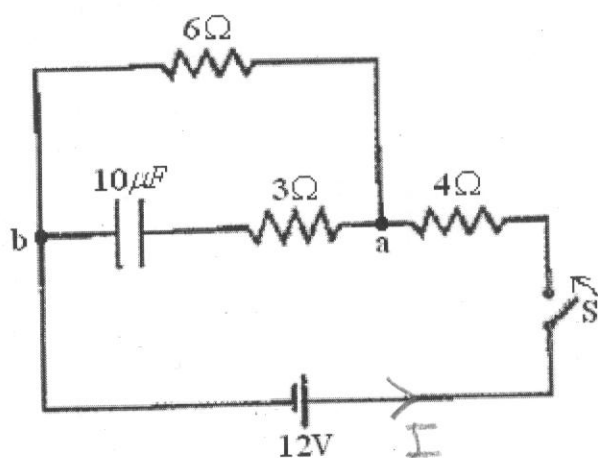
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Consider the circuit given in the figure. The capacitor is initially uncharged and the switch S is closed at  $t=0$ . Long time after ( $t$  goes to infinity) the switch S is closed, find the potential difference  $V_a - V_b$ . What is the maximum charge on the  $10 \mu\text{F}$  capacitor?



\* After we close the circuit, and wait enough, the capacitor gets fully charged. The capacitor behave as open circuit.

The current flows from the outer loop (as  $t \rightarrow \infty$ )

$$I = \frac{12\text{V}}{6\Omega + 4\Omega} = 1,2\text{A}$$

$$V_a - V_b = IR = 1,2\text{A} \times 6\Omega = 7,2\text{V} \quad (\text{point a is @ higher potential})$$

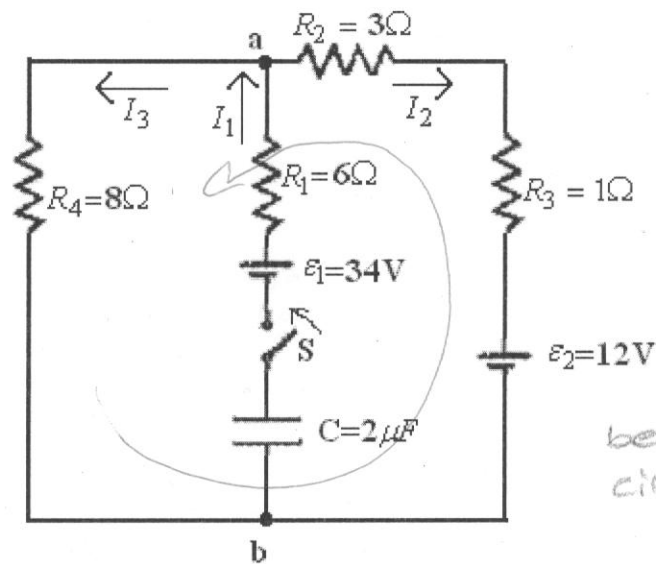
The max. charge on the capacitor is then,

$$Q_{\text{max}} = CV = 10\mu\text{F} \times 7,2\text{V} = 72\mu\text{C}$$

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Consider the circuit in the figure. The capacitor is initially uncharged and the switch S is closed at  $t=0$ . Find the currents  $I_1$ ,  $I_2$  and  $I_3$  long time after ( $t$  goes to infinity) the switch S is closed.



If we wait enough after the switch is closed, the capacitor gets fully charged. The capacitor behaves as an open circuit then.

The current flows from the outer loop only;

$$12V + I_2 \cdot 1\Omega + I_2 \cdot 3\Omega - I_3 \cdot 8\Omega = 0$$

$$4I_2 - 8I_3 = -12V$$

$$2I_3 - I_2 = 3V$$

On the other hand,  $I_1 = I_2 + I_3$  due to junction rule. But  $I_1 = 0$ , since Capacitor behaves as an open circuit. Thus  $I_2 = -I_3$

$$2I_3 - (-I_3) = 3A \Rightarrow 3I_3 = 3A \Rightarrow$$

$I_3 = 1A$
$I_2 = -1A$
$I_1 = 0A$